# Package: QuClu (via r-universe)

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Title Quantile-Based Clustering Algorithms

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Description Various quantile-based clustering algorithms: algorithm CU (Common theta and Unscaled variables), algorithm CS (Common theta and Scaled variables through lambda\_j), algorithm VU (Variable-wise theta\_j and Unscaled variables) and algorithm VW (Variable-wise theta\_j and Scaled variables through lambda\_j). Hennig, C., Viroli, C., Anderlucci, L. (2019) ``Quantile-based clustering." Electronic Journal of Statistics. 13 (2) 4849 -4883 <doi:10.1214/19-EJS1640>.

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alg.CS

# Description

This function allows to run the CS (Common theta and Scaled variables through lambda\_j) version of the quantile-based clustering algorithm.

# Usage

alg.CS(data, k = 2, eps = 1e-08, it.max = 100, B = 30, lambda = rep(1, p))

#### Arguments

data	A numeric vector, matrix, or data frame of observations. Categorical variables are not allowed. If a matrix or data frame, rows correspond to observations and columns correspond to variables.
k	The number of clusters. The default is $k=2$ .
eps	The relative convergence tolerances for objective function. The default is set to 1e-8.
it.max	A number that gives integer limits on the number of the CS algorithm iterations. By default, it is set to 100.
В	The number of times the initialization step is repeated; the default is 30.
lambda	The initial value for lambda_j, the variable scaling parameters. By default, lamb- das are set to be equal to 1.

# Details

Algorithm CS: Common theta and Scaled variables via lambda\_j. A common value of theta is taken but variables are scaled through lambda\_j.

#### Value

A list containing the following elements:

cl	A vector whose [i]th entry is classification of observation i in the test data.
qq	A matrix whose [h,j]th entry is the theta-quantile of variable j in cluster h.
theta	The estimated common theta.
Vseq	The values of the objective function V at each step of the algorithm.
V	The final value of the objective function V.
lambda	A vector containing the scaling factor for each variable.

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#### alg.CU

# References

Hennig, C., Viroli, C., Anderlucci, L. (2019) "Quantile-based clustering" *Electronic Journal of Statistics*, 13 (2) 4849-4883 <doi:10.1214/19-EJS1640>

#### Examples

```
out <- alg.CS(iris[,-5],k=3)
out$theta
out$qq
out$lambda</pre>
```

table(out\$cl)

alg.CU

CU quantile-based clustering algorithm

#### Description

This function allows to run the CU (Common theta and Unscaled variables) version of the quantilebased clustering algorithm.

#### Usage

alg.CU(data, k = 2, eps = 1e-08, it.max = 100, B = 30)

#### Arguments

data	A numeric vector, matrix, or data frame of observations. Categorical variables are not allowed. If a matrix or data frame, rows correspond to observations and columns correspond to variables.
k	The number of clusters. The default is $k=2$ .
eps	The relative convergence tolerances for objective function. The default is set to 1e-8.
it.max	A number that gives integer limits on the number of the CU algorithm iterations. By default, it is set to 100.
В	The number of times the initialization step is repeated; the default is 30.

## Details

Algorithm CU: Common theta and Unscaled variables. A common value of theta for all the variables is assumed. This strategy directly generalizes the conventional k-means to other moments of the distribution to better accommodate skewness in the data.

# Value

A list containing the following elements:

method	The chosen parameterization, CU, Common theta and Unscaled variables
k	The number of clusters.
cl	A vector whose [i]th entry is classification of observation i in the test data.
qq	A matrix whose [h,j]th entry is the theta-quantile of variable j in cluster h.
theta	A vector whose [j]th entry is the percentile theta for variable j.
Vseq	The values of the objective function V at each step of the algorithm.
V	The final value of the objective function V.
lambda	A vector containing the scaling factor for each variable.

#### References

Hennig, C., Viroli, C., Anderlucci, L. (2019) "Quantile-based clustering" *Electronic Journal of Statistics*, 13 (2) 4849-4883 <doi:10.1214/19-EJS1640>

#### Examples

out <- alg.CU(iris[,-5],k=3)
out\$theta
out\$qq</pre>

table(out\$cl)

```
alg.VS
```

VS quantile-based clustering algorithm

#### Description

This function allows to run the VS (Variable-wise theta\_j and Scaled variables through lambda\_j) version of the quantile-based clustering algorithm.

# Usage

alg.VS(data, k = 2, eps = 1e-08, it.max = 100, B = 30, lambda = rep(1, p))

#### Arguments

data	A numeric vector, matrix, or data frame of observations. Categorical variables are not allowed. If a matrix or data frame, rows correspond to observations and columns correspond to variables.
k	The number of clusters. The default is $k=2$ .
eps	The relative convergence tolerances for objective function. The default is set to 1e-8.

# alg.VS

it.max	A number that gives integer limits on the number of the VS algorithm iterations. By default, it is set to 100.
В	The number of times the initialization step is repeated; the default is 30.
lambda	The initial value for lambda_j, the variable scaling parameters. By default, lamb- das are set to be equal to 1.

# Details

Algorithm VS: Variable-wise theta\_j and Scaled variables via lambda\_j. A different theta for every single variable is estimated to better accomodate different degree of skeweness in the data and variables are scaled through lambda\_j.

#### Value

A list containing the following elements:

method	The chosen parameterization, VS, Variable-wise theta_j and Scaled variables
k	The number of clusters.
cl	A vector whose [i]th entry is classification of observation i in the test data.
qq	A matrix whose [h,j]th entry is the theta-quantile of variable j in cluster h.
theta	A vector whose [j]th entry is the percentile theta for variable j.
Vseq	The values of the objective function V at each step of the algorithm.
V	The final value of the objective function V.
lambda	A vector containing the scaling factor for each variable.

## References

Hennig, C., Viroli, C., Anderlucci, L. (2019) "Quantile-based clustering" *Electronic Journal of Statistics*, 13 (2) 4849-4883 <doi:10.1214/19-EJS1640>

#### Examples

```
out <- alg.VS(iris[,-5],k=3)
out$theta
out$qq
out$lambda
table(out$cl)</pre>
```

#### alg.VU

#### Description

This function allows to run the VU (Variable-wise theta\_j and Unscaled variables) version of the quantile-based clustering algorithm.

#### Usage

alg.VU(data, k = 2, eps = 1e-08, it.max = 100, B = 30)

#### Arguments

data	A numeric vector, matrix, or data frame of observations. Categorical variables are not allowed. If a matrix or data frame, rows correspond to observations and columns correspond to variables.
k	The number of clusters. The default is $k=2$ .
eps	The relative convergence tolerances for objective function. The default is set to 1e-8.
it.max	A number that gives integer limits on the number of the VU algorithm iterations. By default, it is set to 100.
В	The number of times the initialization step is repeated; the default is 30.

### Details

Algorithm VU: Variable-wise theta\_j and Unscaled variables. A different theta for every single variable is estimated to better accomodate different degree of skeweness in the data.

#### Value

A list containing the following elements:

method	The chosen parameterization, VU, Variable-wise theta_j and Unscaled variables
k	The number of clusters.
cl	A vector whose [i]th entry is classification of observation i in the test data.
qq	A matrix whose [h,j]th entry is the theta-quantile of variable j in cluster h.
theta	A vector whose [j]th entry is the percentile theta for variable j.
Vseq	The values of the objective function V at each step of the algorithm.
V	The final value of the objective function V.
lambda	A vector containing the scaling factor for each variable.

#### References

Hennig, C., Viroli, C., Anderlucci, L. (2019) "Quantile-based clustering" *Electronic Journal of Statistics*, 13 (2) 4849-4883 <doi:10.1214/19-EJS1640>

#### kquantiles

# Examples

```
out <- alg.VU(iris[,-5],k=3)
out$theta
out$qq</pre>
```

table(out\$cl)

```
kquantiles
```

Quantile-based clustering algorithm

# Description

This function allows to run the \$k\$-quantile clustering algorithm, allowing for different constraints: common theta and unscaled variables (CU), common theta and scaled variables (CS), variable-wise theta and unscaled variables (VU) and the variable-wise theta and scaled variables (VS).

# Usage

```
kquantiles(
    data,
    k = 2,
    method = "VS",
    eps = 1e-08,
    it.max = 100,
    B = 30,
    lambda = NULL
)
```

#### Arguments

data	A numeric vector, matrix, or data frame of observations. Categorical variables are not allowed. If a matrix or data frame, rows correspond to observations and columns correspond to variables.
k	The number of clusters. The default is $k=2$ .
method	The chosen constrained method. The options are: CU (Common theta and Unscaled variables), CS (Common theta and Scaled variables), VU (Variable- wise theta and Unscaled variables), VS (Variable-wise theta and Scaled variables). The default is the unconstrained method, VS.
eps	The relative convergence tolerances for objective function. The default is set to 1e-8.
it.max	A number that gives integer limits on the number of the algorithm iterations. By default, it is set to 100.
В	The number of times the initialization step is repeated; the default is 30.
lambda	The initial value for lambda_j, the variable scaling parameters, for models CS and VS. By default, lambdas are set to be equal to 1.

#### Details

Algorithm CU: Common theta and Unscaled variables. A common value of theta for all the variables is assumed. Algorithm CS: Common theta and Scaled variables via lambda\_j. A common value of theta is taken but variables are scaled through lambda\_j. Algorithm VU: Variable-wise theta\_j and Unscaled variables. A different theta for every single variable is estimated to better accomodate different degree of skeweness in the data. Algorithm VS: Variable-wise theta\_j and Scaled variables via lambda\_j. A different theta for every single variable is estimated to better accomodate different degree of skeweness in the data and variables are scaled through lambda\_j.

#### Value

A list containing the following elements:

method	The chosen parameterization.
k	The number of clusters.
cl	A vector whose [i]th entry is classification of observation i in the test data.
qq	A matrix whose [h,j]th entry is the theta-quantile of variable j in cluster h.
theta	A vector whose [j]th entry is the percentile theta for variable j.
Vseq	The values of the objective function V at each step of the algorithm.
V	The final value of the objective function V.
lambda	A vector containing the scaling factor for each variable.

#### References

Hennig, C., Viroli, C., Anderlucci, L. (2019) "Quantile-based clustering" *Electronic Journal of Statistics*, 13 (2) 4849-4883 <doi:10.1214/19-EJS1640>

#### Examples

```
out <- kquantiles(iris[,-5],k=3,method="VS")
out$theta
out$qq</pre>
```

table(out\$cl)

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